

Variability analysis in memristors based on electrodeposited prussian blue

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ABSTRACT

This work presents a comprehensive analysis of the variability and reliability of the resistive switching (RS) behavior in Prussian Blue (a mixed-valence iron(III/II) hexacyanoferrate compound) thin films, used as the active layer. These films are fabricated through a simple and scalable electrochemical process, and exhibit robust bipolar resistive switching, making them suitable both for neuromorphic computing applications and hardware cryptography. A detailed statistical evaluation was conducted over 100 consecutive switching cycles using multiple parameter extraction techniques to assess cycle-to-cycle (C2C) variability in key RS parameters, including set/reset voltages and corresponding currents. One and two-dimensional coefficients of variation (1DCV and 2DCV) were calculated to quantify variability and identify application potential. Results demonstrate moderate variability compatible with neuromorphic computing and cryptographic functionalities, including physical unclonable functions and true random number generation. These findings position Prussian Blue-based memristors as promising candidates for low-cost, stable, and multifunctional memory.

1. Introduction

Memristors, a new kind of electron devices [17,18] that shows hysteresis in their current versus voltage curves linked to its materials properties, are drawing attention from the electronics industry due to the great potential of their outstanding applications [28,29]. The most straightforward use of these devices is found in the non-volatile memory realm [15,53,57]. The resistive switching (RS) features of memristors allow multilevel operation [41,42,45], as is the case in conventional Flash technology. In this respect, different foundries and IC companies, such as TSMC and INTEL, have shown the correct operation of non-volatile memory chips in the context of the 22 nm technology [16,24]. In the field of cryptography, the inherent stochastic behavior of these devices allows the fabrication of hardware solutions for the implementation of entropy sources for true random number generators [56], or physical unclonable functions [37]. In addition, the memristive device internal dynamics can mimic the operation of biological synapses, accounting for the ionic transport that triggers RS [32,34,36,47,54].

Consequently, these devices play a key role in neuromorphic engineering, a subject introduced in the late eighties by Carver Mead [33]. Memristors are essential in the implementation of crossbar arrays that can optimize vector-matrix multiplication, a crucial operation for the acceleration of training and inference processes in hardware neural networks [7,8,20,23,35,41,44,52,58,59].

Despite their game-changing applications, some issues need to be addressed to improve memristor technologies, e.g. the lack of accurate modeling and simulation tools to aid in the device and circuit design [27,46]. Variability, both in the cycle-to-cycle [22,30,48,49] and device-to-device [40] flavors, also needs improvement. In particular, in what is connected to the statistical analysis of data and in compact modeling to build reliable circuit simulators and other EDA tools for integrated circuit design. In order to reduce variability and advance in other facets such as endurance, retention, etc., different materials have been employed to build the device stack. In this context, new electrodes and mostly, dielectrics, are being studied, such as transition-metal oxides [28,39,43,53], two-dimensional (2D) layered materials, boron-

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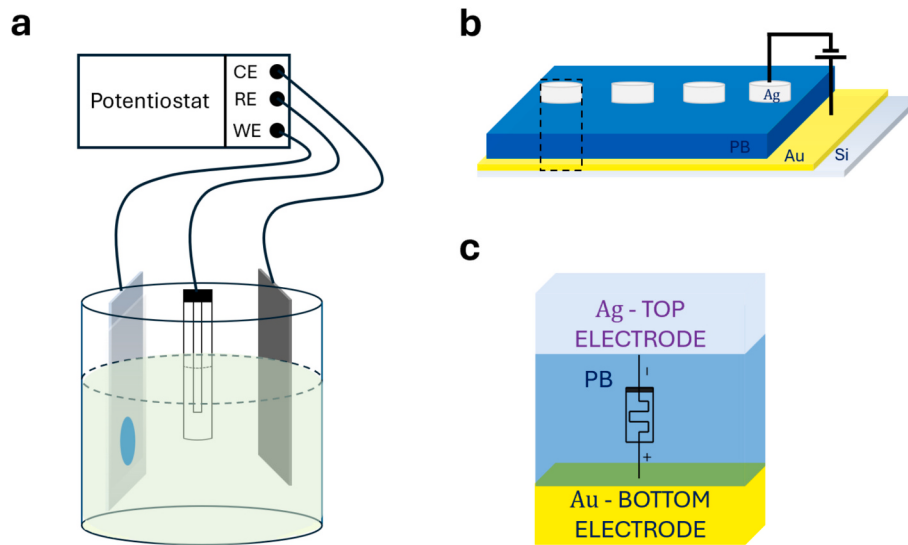


Fig. 1. **a** Schematic of the experimental setup for the electrochemical deposition of PB thin films, showing the Counter Electrode (CE, Pt), Reference Electrode (RE), Working Electrode (WE), and the electrolyte (depicted in green). **b** Schematic representation of the sample's layer sequence and electrode configuration used for electrical measurements. **c** Close-up view of a single PB vertical memristor.

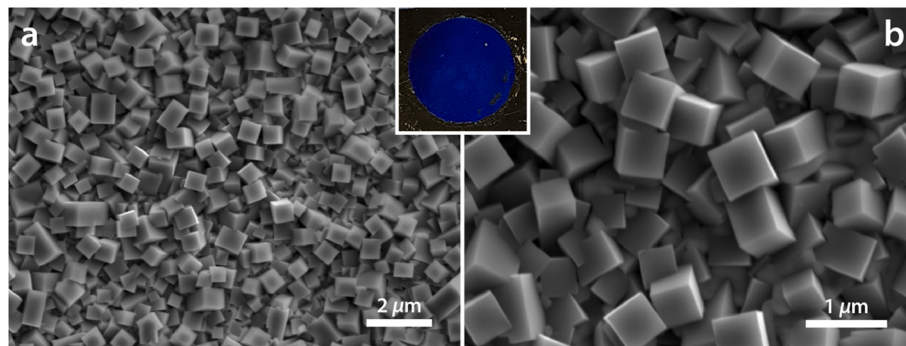


Fig. 2. SEM images of the PB layer electrodeposited at 0.3 V obtained at 10 keV. **a** Surface overview, photograph image of the film (inset), **b** a more detailed view of the film surface.

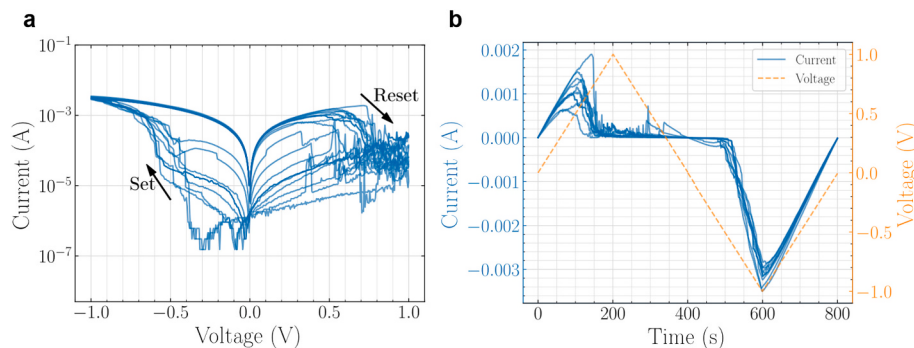


Fig. 3. **a** Representative RS I-V curves illustrate the transition between HRS and LRS and the other way around. We have included the 1st measurement, the 10th, 20th... till the 100th measurement. **b** Current and voltage transients over time for the curves shown in panel a.

based compounds [26], MXenes [25], perovskites and nanotubes [13,38], quantum dots and polymers [4,51], etc.

Resistive Random-Access Memories (RRAM) are counted among memristive devices [19]. Their simple metal-oxide-metal structure allows them to be fabricated in the BEOL of CMOS integrated circuits [59]. In the context highlighted above, we present here a variability study of RRAMs where a new material is considered as the dielectric, the

Prussian Blue (PB) [1–3,21].

Prussian Blue is a mixed-valence iron(III/II) hexacyanoferrate compound, renowned for its distinctive cubic face-centered structure. In its crystal lattice, Fe^{3+} ions are coordinated by nitrogen atoms, while Fe^{2+} ions are coordinated by carbon atoms, forming the repeating bonding chain $Fe^{3+}-N \equiv C-Fe^{2+}-C \equiv N-Fe^{3+}$. This well-ordered structure not only causes the material's characteristic deep blue color but also endows

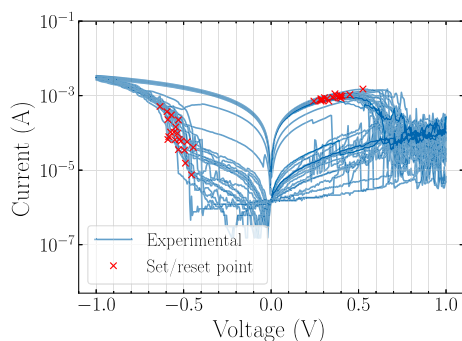


Fig. 4. Representative current versus voltage curves for the devices under study. The set and reset voltages are shown in red crosses in the curves. The ramped voltage employed in the measurements had a slope of 5 mV/s.

it with unique physical and chemical properties [14]. Substitution of iron ions with other transition metal ions (e.g. cobalt or manganese) gives rise to a broader class of materials known as Prussian Blue analogs (PBAs) [12]. Electrodeposition is a highly versatile technique for depositing PB onto conductive substrates from an aqueous electrolyte solution. This method offers exceptional flexibility, as it is compatible with various metals and adaptable to different device sizes. Such advantages make it particularly suitable for wafer-scale device integration. In this work, Prussian Blue thin films were synthesized via electrodeposition, and their morphological and electrical properties were systematically investigated to evaluate their potential for device applications. An in-depth variability study is performed from the statistical viewpoint.

The device fabrication details, and measurement setup are described in section 2, the variability statistical study is given in section 3, and the conclusions are drawn in section 4.

2. Device fabrication and measurement setup

The electrochemical deposition of prussian blue (PB) films was

carried out in potentiostatic mode using an electrochemical workstation (Ivium CompactStat, Eindhoven, Netherlands) at room temperature. The electrochemical system used for the fabrication of PB is presented in Fig. 1a, where the working electrode (WE) consists of Au/Cr/Si substrates. At the same time, a Pt foil served as the counter electrode (CE) and a saturated calomel electrode (SCE), as the reference electrode (RE), all connected to the Potentiostat. The working electrode was fabricated by evaporating 50 nm of Au onto a 5 nm Cr layer on (100) Si substrates (1 cm × 1 cm) at a base pressure of 10^{-5} Pa. PB deposition occurred within a 0.5 cm² circular area, defined by an adhesive tape mask.

The electrolyte solution for electrochemical synthesis consisted of 1.0 M KCl, 5.0 mM HCl, 0.5 mM FeCl₃, and 0.5 mM K₃Fe(CN)₆, all dissolved in 100 mL of deionized water, with the pH adjusted to 2. All chemicals (Sigma Aldrich, Darmstadt, Germany) had a purity of >99 %. PB layers were deposited by applying a constant potential of 0.3 V between the WE and CE at 25 °C. The electrodeposition process was carefully controlled by limiting the total deposited charge to 30 mC, which corresponds to an estimated PB layer thickness of approximately 500 nm. The correlation between deposition charge and film thickness for electrodeposited PB is well established in the literature, enabling precise control over the film growth [1,2,9,21]. The sample morphology was characterized using field emission scanning electron microscopy (FEG-SEM; TESCAN CLARA, Brno, Czech Republic). As shown in Fig. 2, the PB film electrodeposited exhibits a well-defined cubic crystal morphology, with a highly ordered structure matching PB's intrinsic face-centered cubic (fcc) structure. The film displays a compact and homogeneous grain distribution across the substrate (Inset photo). Small clusters composed of aggregated cubes were also observed on the surface (Fig. 2).

The study of these devices based on Prussian blue is at the prototype level currently, further improvements would be needed to face the issues related to wafer level fabrication.

To investigate the RS effect, current-voltage (I-V) characterization was performed using a Keithley 2400 programmable electrometer. The measurements were conducted with a two-point probe configuration. The device structure consisted of a PB film sandwiched between a top silver (Ag) electrode and a bottom gold (Au) electrode, forming a metal-

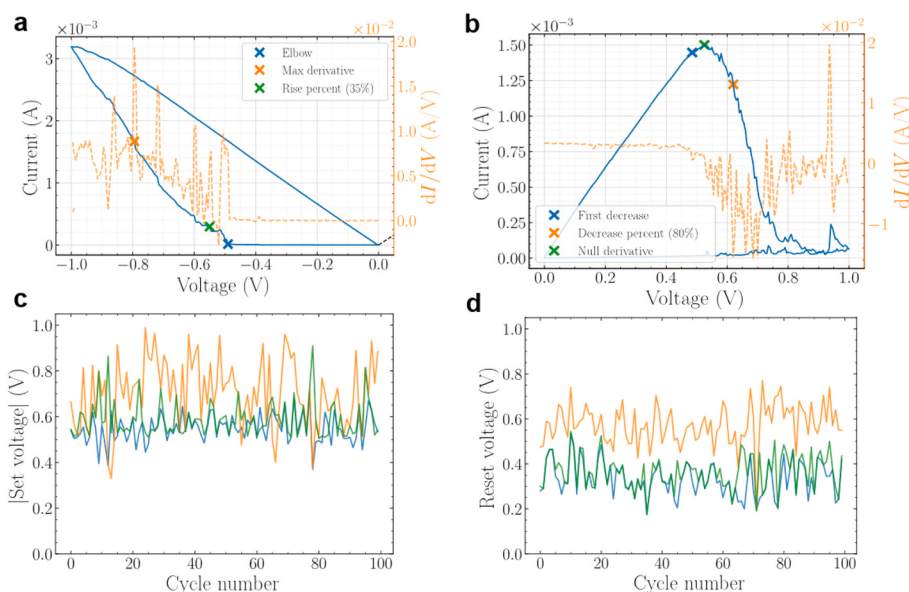


Fig. 5. **a** Set current versus voltage curve where the three set voltage extraction procedures employed are shown [31]. Determination of the maximum current increase (35 %) between two consecutive current points (green crosses, MS1), maximum separation of the experimental I-V curve with a straight line that joins the first and final points of the I-V curve (blue crosses, MS2, elbow method) and maximum current derivative in the current curve (orange crosses, MS3). **b** Reset current versus voltage curve showing the three reset voltage extraction procedures used [31]. Calculation of the first current decrease along the I-V curve (blue crosses, MR1), minimum (or null) current derivative along the curve (green crosses, MR2), and maximum decrease (20 %) in two consecutive current points (orange crosses, MR3). **c** **(d)** Set absolute value (reset) voltage versus the number of cycles for the prussian blue based devices.

Table 1

a (b) Tables with the 1DCV for the set (reset) voltages for prussian blue devices. c (d) Tables with the 2DCV for the set (reset) voltages for Prussian Blue devices. The pairs of variables employed were (V_{set} , I_{set}) and (V_{reset} , I_{reset}). e Table with the 2DCV for (V_{set} , V_{reset}). The CV are obtained for the different extraction techniques employed in the study [31].

a		
1D CV, Set		
Method		CV
Elbow		0.113
Max derivative		0.207
Rise percent (35%)		0.136

b		
1D CV, Reset		
Method		CV
First decrease		0.228
Decrease percent (80%)		0.152
Null derivative		0.213

c		
2D CV, (V_{set} , I_{set})		
Method		CV
Elbow		0.070
Max derivative		0.160
Rise percent (35%)		0.093

d		
2D CV, (V_{reset} , I_{reset})		
Method		CV
First decrease		0.078
Decrease percent (80%)		0.089
Null derivative		0.080

e		
2D CV, (V_{set} , V_{reset})		
Method		CV
Elbow	First decrease	0.100
Elbow	Decrease percent (80%)	0.109
Elbow	Null derivative	0.101
Max derivative	First decrease	0.169
Max derivative	Decrease percent (80%)	0.174
Max derivative	Null derivative	0.170
Rise percent (35%)	First decrease	0.113
Rise percent (35%)	Decrease percent (80%)	0.120
Rise percent (35%)	Null derivative	0.114

insulator-metal (MIM) structure essential for resistive switching characterization. The bottom Au electrode served as the fixed contact, providing a stable and uniform interface for the PB film, while the top Ag electrode was prepared by drop casting directly applied onto the PB surface. Fig. 1b illustrates the complete structure, while Fig. 1c presents the structure of a single memristor.

Electrical characterization, specifically current-voltage (I-V) measurements, was performed on the devices using the same electrochemical workstation used for electrodeposition. A DC voltage sweep ranging from -1 V to $+1$ V was applied at a scan rate of 5 mV/s during the measurement. Fig. 3a displays the current as a function of the applied voltage for the first curve, the 10th, the 20th ... and the 100th of a RS series under the ramp voltage stress regime, revealing a

characteristic butterfly-shaped curve. The devices show a forming free characteristic, as well as stability and repeatability over multiple cycles. In the positive polarity, the transition from the low-resistance state (LRS) to the high-resistance state (HRS) is observed, indicating the Reset process. The device remains in the HRS until the polarity is reversed. Upon applying negative bias, the transition from HRS to LRS occurs, corresponding to the Set process.

As shown in Fig. 3b, the current transient and applied voltage are plotted as a function of time, a complete switching cycle takes 800 s. In this study, we employ slower scan rates to minimize device stress, ensuring more reliable and repeatable results, an essential factor for assessing long-term stability and endurance. Additionally, a reduced scan rate helps suppress capacitive and transient effects, making the resistive component of the current more prominent. By allowing sufficient time for the necessary physical or chemical changes to occur, the slower scan rate enables a more accurate observation of the device's intrinsic switching behavior, leading to a clearer representation of its switching kinetics.

3. Variability statistical study

As shown in Fig. 3a, these devices exhibit two well-defined states (HRS and LRS), making them good candidates for non-volatile memories or neuromorphic applications. However, the C2C variability requirements for each of these applications are different. Therefore, a thorough analysis of their variability is required to accurately identify this technology potential.

Fig. 4 shows some I-V curves of a RS series for the devices under study. The set voltages (V_{set}) and reset voltages (V_{reset}) are marked with red crosses in the curves, 100 complete I-V curves have been analyzed. The corresponding current values, I_{set} and I_{reset} , are found in the experimental I-V curves and correspond to V_{set} and V_{reset} .

For the RS parameter extraction, we employed three different numerical procedures, see Ref. [31,55]. V_{set} was obtained by means of (MS1 technique in [31]) the determination of the maximum current increase (35 %) between two consecutive current points, the MS2 technique extracts the set I-V curve elbow; finally, the MS3 technique is based on the determination of the maximum current derivative along the curve, see Fig. 5a. V_{reset} was obtained (MR1) through the first current decrease along the I-V curve, the MR2 technique is connected to the minimum (or null) current derivative along the current curve, and the MR3 technique extracts the maximum current decrease (80 %) in two consecutive current points, see Fig. 5b.

Making use of these data, an in-depth statistical study on cycle-to-cycle (C2C) variability is performed by using the coefficient of variation (CV) in several dimensions [6]. The one-dimensional version of this coefficient (1DCV, defined as σ/μ , where σ stands for the standard deviation and μ is the mean) and the two-dimensional CV (2DCV) [5,6] are shown in Table 1, calculated considering the pairs of values (V_{reset} , I_{reset}) or (V_{set} , I_{set}). The 1DCV has been used in the past for the analysis of the C2C variability. For $1\text{DCV}(V_{\text{set}}) < 2\%$, the devices are recommended for information storage [15]; although higher values could be employed in the neuromorphic computation context [52]. For $1\text{DCV}(V_{\text{set}}) > 20\%$, the devices could be employed for data encryption, as an entropy source of true random number generators [56], or physical unclonable functions [37].

The 2DCV is higher for the set voltage (Table 1c) with respect to the reset voltage (Table 1d). Nevertheless, the 1DCV for the set voltage (Table 1a) is lower, in general, than for the reset voltage (Table 1b). These statistical effects (different trends for the 1DCVs and 2DCVs) have been observed previously [6]; in this respect, a 2D dataset produces a much more accurate analysis.

According to the results shown in Table 1, our devices could be used for neuromorphic computing and cryptographic applications in the current development state [48]. It is important to highlight that, in the context of neuromorphic computing, variability can be beneficial to

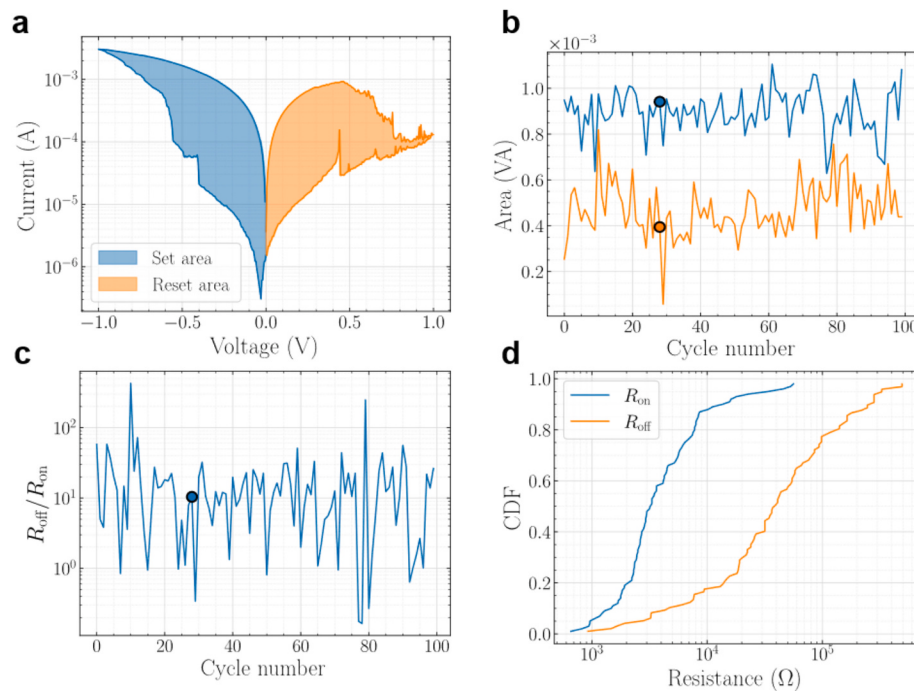


Fig. 6. Current versus voltage curves measured under RVS. **a** The area included within the curves is shown in blue for the set process and orange for the reset process. **b** Area included in the I-V curves versus cycle number for the RS series we have measured. The dots mark the cycle corresponding to panel **a**. **c** $R_{\text{off}}/R_{\text{on}}$ ratio versus cycle number. The dot marks the cycle corresponding to the I-V curves of panel **a**. **d** Cumulative distribution function for the R_{off} and R_{on} . R_{on} was extracted in the LRS for a voltage of -0.3 V, R_{off} was obtained in the HRS for a voltage of 0.3 V.

overcome problems such as a lack of precision in neural network recognition due to overfitting [50].

A different perspective can be obtained by studying the area included between the LRS and HRS parts of the I-V curve (see Fig. 6a). The evolution of this area in the RS series is shown in Fig. 6b. A nonzero area within the RS loop assures the device I-V curve hysteresis and, consequently, the memory effects [11]. This parameter could be employed for modeling purposes [10,11] since it is related to the action potential, which was introduced by Leon Chua in his original work [17]. See that the area value through the RS series is maintained reasonably well (save variability effects) (Fig. 6b); therefore, the non-volatile memory potential does not decline as the number of cycles increases, as required for memory applications.

A more conventional analysis to assess the appropriateness of this technology for non-volatile memory applications is linked to the evaluation of the $R_{\text{off}}/R_{\text{on}}$ ratio, measured at ± 0.3 V (Fig. 6c). Although a 10-factor is achieved on average, an improvement in the C2C variability is still needed because for some cycles the $R_{\text{off}}/R_{\text{on}}$ ratio falls below 1. The cumulative distribution functions are shown in Fig. 6d to shed light on this issue.

4. Conclusions

In this study, we have demonstrated the feasibility of using electro-deposited Prussian Blue thin films as an active material for memristive devices, highlighting their potential for RS applications. Through an extensive statistical variability analysis over 100 switching cycles, we identified stable bipolar RS behavior and extracted critical performance parameters using multiple data processing techniques. The calculated coefficients of variation reveal that these devices are suitable for applications in neuromorphic computing and hardware-based cryptography. The consistent switching area and stable hysteresis loops observed over multiple cycles show the great potential of Prussian Blue devices for resistive switching operation.

CRediT authorship contribution statement

L.B. Avila: Conceptualization, Investigation, Visualization, Data curation, Writing – original draft, Writing – review & editing. **A. Canto:** Investigation, Data curation, Validation, Formal analysis, Visualization. **M.A. Villena:** Investigation. **D. Maldonado:** Investigation. **F. Abreu Araujo:** Writing – review & editing, Funding acquisition. **C.K. Müller:** Writing – review & editing, Funding acquisition. **J.B. Roldán:** Investigation, Conceptualization, Validation, Writing – original draft, Writing – review & editing, Funding acquisition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Data availability

The datasets generated and/or analyzed during the current study are available from the corresponding author on reasonable request.

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